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Date: 28 January 2018 Time : **09:00-12:00 (3 hours)**
 Roll Number:
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Maximum Marks: 75

I **permit/do not permit** (*strike out one*) HBCSE to reveal my academic performance and personal details to a third party.

Besides the International Physics Olympiad (IPhO) 2018, do you also want to be considered for the Asian Physics Olympiad (APhO) 2018? For APhO 2018 and its pre-departure training, your presence will be required in Delhi and Vietnam from April 28 to May 15, 2018. In principle, you can participate in both Olympiads. Yes/No.

Full Name (BLOCK letters) Ms./Mr.: _

Extra sheets attached :	$\overline{\text{Date}}$	Centre (e.g. Kochi)	Signature
	<u>(Do_not_u</u>	vrite_below_this_line)	

Instructions

- 1. This booklet consists of 27 pages (excluding this sheet) and total of 7 questions.
- 2. This booklet is divided in two parts: Questions with Summary Answer Sheet and Detailed Answer Sheet. Write roll number at the top wherever asked.
- 3. The final answer to each sub-question should be neatly written in the box provided below each sub-question in the Questions & Summary Answer Sheet.
- 4. You are also required to show your **detailed work** for each question in a reasonably neat and coherent way in the **Detailed Answer Sheet**. You must write the relevant Question Number(s) on each of these pages.
- 5. Marks will be awarded on the basis of what you write on both the Summary Answer Sheet and the Detailed Answer Sheet. Simple short answers and plots may be directly entered in the Summary Answer Sheet. Marks may be deducted for absence of detailed work in questions involving longer calculations. Strike out any rough work that you do not want to be considered for evaluation.
- 6. Adequate space has been provided in the answersheet for you to write/calculate your answers. In case you need extra space to write, you may request additional blank sheets from the invigilator. Write your roll number on the extra sheets and get them attached to your answersheet and indicate number of extra sheets attached at the top of this page.
- 7. Non-programmable scientific calculators are allowed. Mobile phones **cannot** be used as calculators.
- 8. Use blue or black pen to write answers. Pencil may be used for diagrams/graphs/sketches.
- 9. This entire booklet must be returned at the end of the examination.

			Question	Marks	Score
Table of Co	onsta	nts			
Speed of light in vacuum	c	$3.00\times10^8~{\rm m\cdot s^{-1}}$	1	4	
Planck's constant	h	$6.63 \times 10^{-34} \text{ J} \cdot \text{s}$			
	\hbar	$h/2\pi$	2	8	
Universal constant of Gravitation	G	$6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2 \cdot \text{kg}^{-2}$	2	10	
Magnitude of electron charge	e	$1.60 \times 10^{-19} \text{ C}$	3	12	
Rest mass of electron	m_e	$9.11 \times 10^{-31} \text{ kg}$		0	
Rest mass of proton	m_p	$1.67 \times 10^{-27} \text{ kg}$	4	9	
Value of $1/4\pi\epsilon_0$		$9.00 \times 10^9 \text{ N} \cdot \text{m}^2 \cdot \text{C}^{-2}$	-	10	
Avogadro's number	N_A	$6.022 \times 10^{23} \mathrm{mol}^{-1}$	5	10	
Acceleration due to gravity	g	$9.81 \text{ m} \cdot \text{s}^{-2}$	0		
Universal Gas Constant	R	$8.31 \text{ J} \cdot \text{K}^{-1} \cdot \text{mol}^{-1}$	6	17	
Molar mass of water		$18.02 \mathrm{g} \cdot \mathrm{mol}^{-1}$	_		
Permeability constant	μ_0	$4\pi \times 10^{-7}$ H·m ⁻¹	7	15	
			Total	75	

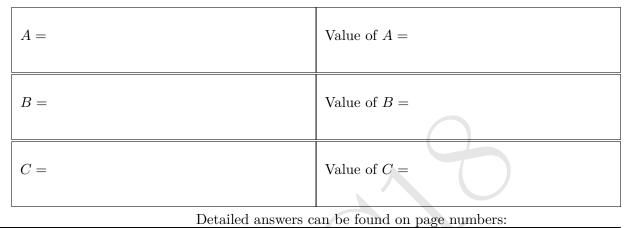
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INPhO 2018 Page 1 Questions & Summary Answers

1. In a nucleus, the attractive central potential which binds the proton and the neutron is called [4] the Yukawa potential. The associated potential energy U(r) is

$$U(r) = -\alpha \frac{e^{-r/\lambda}}{r}$$

Here $\lambda = 1.431 \text{ fm}$ (fm = 10^{-15} m), r is the distance between nucleons, and $\alpha = 86.55 \text{ MeV} \cdot \text{fm}$ is the nuclear force constant (1 MeV = $1.60 \times 10^{-13} \text{ J}$). Assume nuclear force constant α to be $A\hbar c$. Here $\hbar = h/2\pi$ and h is Planck's constant. In order to compare the nuclear force to other fundamental forces of nature within the nucleus of Deuterium (²H), let the constants associated with the electrostatic force and the gravitational force to be equal to $B\hbar c$ and $C\hbar c$ respectively. Here A, B and C are dimensionless. State the expression and numerical values of A, B and C.



- 2. An opaque sphere of radius R lies on a horizontal plane. On the perpendicular through the point of contact, there is a point source of light at a distance R above the top of the sphere (i.e. 3R from the plane).
 - (a) Find the area of the shadow of the sphere on the plane.

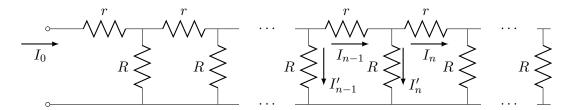
Area =

(b) A transparent liquid of refractive index $\sqrt{3}$ is filled above the plane such that the sphere is just covered with liquid. Find the area of the shadow of the sphere on the plane now.

Area =

Detailed answers can be found on page numbers:

3. Consider an infinite ladder of resistors. The input current I_0 is indicated in the figure.



(a) Find the equivalent resistance of the ladder.

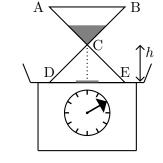
Equivalent resistance =

[2]

[6]

Questions & Summary Answers INPhO 2018 Page 2 Last four digits of Roll No.: (b) Find the recursion relation obeyed by the currents through the horizontal resistors r. You $[\mathbf{2}]$ will get a relationship where I_n will be related to (may be several) I_i s, i < n, n > 0. Relation : (c) Solve this for the special case R = r to obtain I_n and I'_n as explicit functions of n. You may [4] have to make a reasonable assumption about the behaviour of I_n as n becomes large. $I_n =$ $I'_n =$ (d) If the ladder is chopped off after the N-th node (so that $I_{N+1} = 0$) what will the form of [4] $\frac{I_n}{I_N}$ be for $n \le N$? $\frac{I_n}{I_N} =$

4. An hour glass is placed on a weighing scale. Initially all the sand of mass m_0 kg in the glass is held in the upper reservoir (ABC) and the mass of the glass alone is M kg. At t = 0, the sand is released. It exits the upper reservoir at constant rate $\frac{dm}{dt} = \lambda$ kg/s where m is the mass of the sand in the upper reservoir at time t sec. Assume that the speed of the falling sand is zero at the neck of the glass and after it falls through a constant height hit instantaneously comes to rest on the floor (DE) of the hour glass. Obtain the reading on the scale for all times t > 0. Make a detailed plot of the reading vs time.



[9]

Reading on the scale :

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Reading (kg)			
		\bigcirc	time

Detailed answers can be found on page numbers:

5. (a) Consider two short identical magnets each of mass M and each of which maybe considered as point dipoles of magnetic moment \$\vec{\mu}\$. One of them is fixed to the floor with its magnetic moment pointing upwards and the other one is free and found to float in equilibrium at a height z above the fixed dipole. The magnetic field due to a point dipole at a distance r from it is

$$\vec{B}(\vec{r}) = \frac{\mu_0}{4\pi r^3} (3(\vec{\mu} \cdot \hat{r})\hat{r} - \vec{\mu})$$

Obtain an expression for the magnitude of the dipole moment of the magnet in terms of z and related quantities.

$$\vec{\mu} =$$

(b) i. Consider a ring of mass M_r rotating with uniform angular speed about its axis. A [1½] charge q is smeared uniformly over it. Relate its angular momentum $\vec{S_r}$ to its magnetic moment $(\vec{\mu_r})$.

$$\vec{\mu_r} =$$

ii. Assume that the electron is a sphere of uniform charge density rotating about its diameter with constant angular speed. Also assume that the same relation as in the previous part holds between its angular momentum \vec{S} and its magnetic dipole moment ($\vec{\mu}_{\rm B}$). Further assume that $S = h/(2\pi)$ where h is Planck's constant. Calculate μ_B .

 $\mu_{\rm B} =$

iii. Assume that the sole contribution to the dipole moment of a ZnFe_2O_4 molecule comes from an unpaired electron. Also assume that the magnets in the part (5a) are 0.482 kg each of ZnFe_2O_4 and the unpaired electrons of the molecules are all aligned. Calculate the height z. (Note: The molecular weight of $\text{ZnFe}_2\text{O}_4 = 211$)

|z =

[1]

[3]

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iv. In an experiment μ_B is aligned along a magnetic field of 1 T. It is flipped in a direction [1½] anti-parallel to the magnetic field by an incident photon. What should be the wavelength of this photon?

Wavelength =

Detailed answers can be found on page numbers:

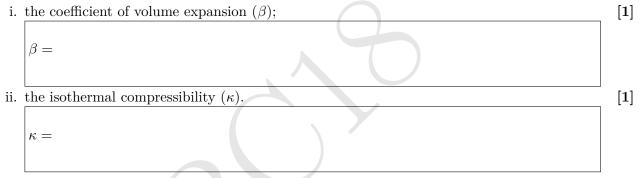
6. The Van der Waals Gas:

Consider n mole of a non-ideal (realistic) gas. Its equation of state maybe described by the Van der Waals equation

$$\left(P + \frac{an^2}{V^2}\right)\left(\frac{V}{n} - b\right) = RT$$

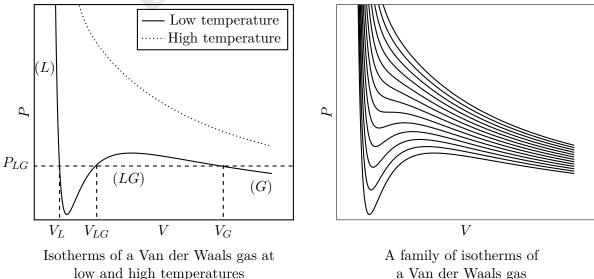
where a and b are positive constants. We take one mole of the gas (n = 1). You must bear in mind that one is often required to make judicious approximations to understand realistic systems.

(a) For this part only take a = 0. Obtain expressions in terms of V, T and constants for



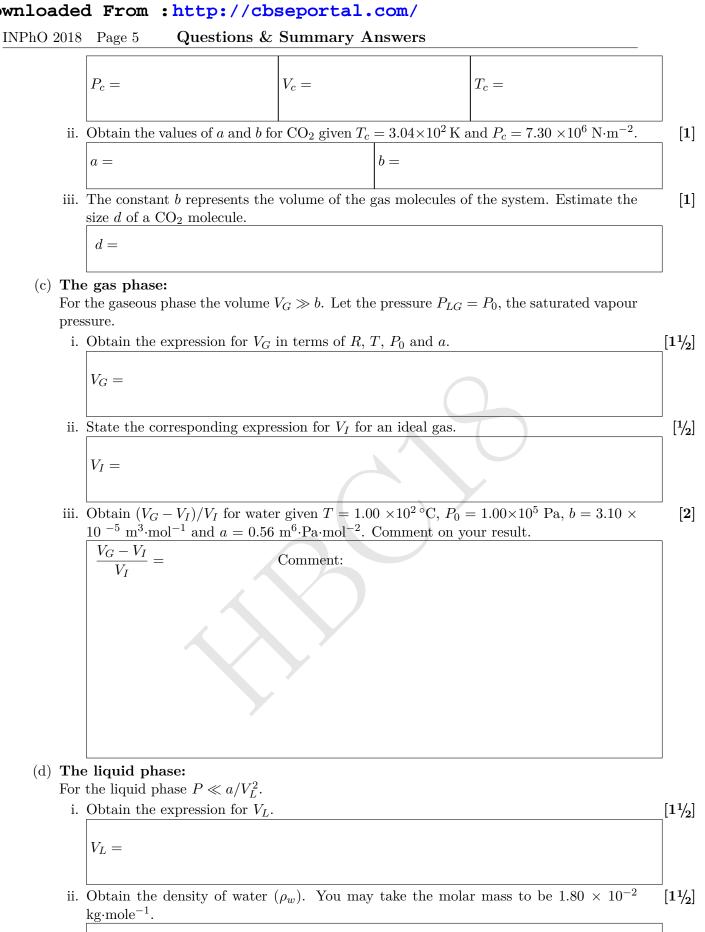
(b) Criticality:

The Van der Waals gas exhibits phase transition. A typical isotherm at low temperature is shown in the figure. Here L(G) represents the liquid (gas) phase and at P_{LG} there are three possible solutions for the volume (V_L, V_{LG}, V_G) . As the temperature is raised, at a certain temperature T_c , the three values of the volume merge to a single value, V_c (corresponding pressure being P_c). This is called the point of criticality. As the temperature is raised further there exists only one real solution for the volume and the isotherm resembles that of an ideal gas.



i. Obtain the critical constants P_c , V_c and T_c in terms of a, b and R.

[4]

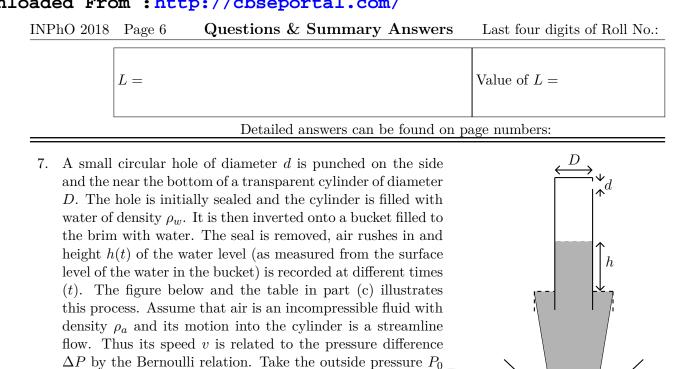


iii. The heat of vaporization is the energy required to overcome the attractive intermolecular force as the system is taken from the liquid phase (V_L) to the gaseous phase (V_G) . The term a/V^2 represents this. Obtain the expression for the specific heat of vaporization per unit mass (L) and obtain its value for water.

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 $\rho_w =$

[2]



to be atmospheric pressure = 1.00×10^5 Pa.

(a) Obtain the dependence of the instantaneous speed v_w of the water level in the cylinder on

$$v_w =$$

h.

(b) Obtain the dependence of h on time.

h =

 $10^3 \, \text{kg/m}^3$ obtain

(c) The table gives the height h as function of time t. Draw a suitable linear graph (t on x axis) from this data on the graph paper provided. Two graph papers are provided with this booklet in case you make a mistake.

$h(\mathrm{cm})$
21.54
20.10
18.67
17.23
15.80
14.36
12.92
11.49

- (d) From the graph and the following data: $D = 6.66 \,\mathrm{cm}, \,\rho_a = 1.142 \,\mathrm{kg/m^3}, \,\rho_w = 1.000 \,\times$ [5]
 - i. The height h_0 at t = 0. $h_0 =$ ii. The value of d. d =iii. The initial speed (v_w) of the water level. $v_w(t=0) =$

Detailed answers can be found on page numbers:

[3]

[4]

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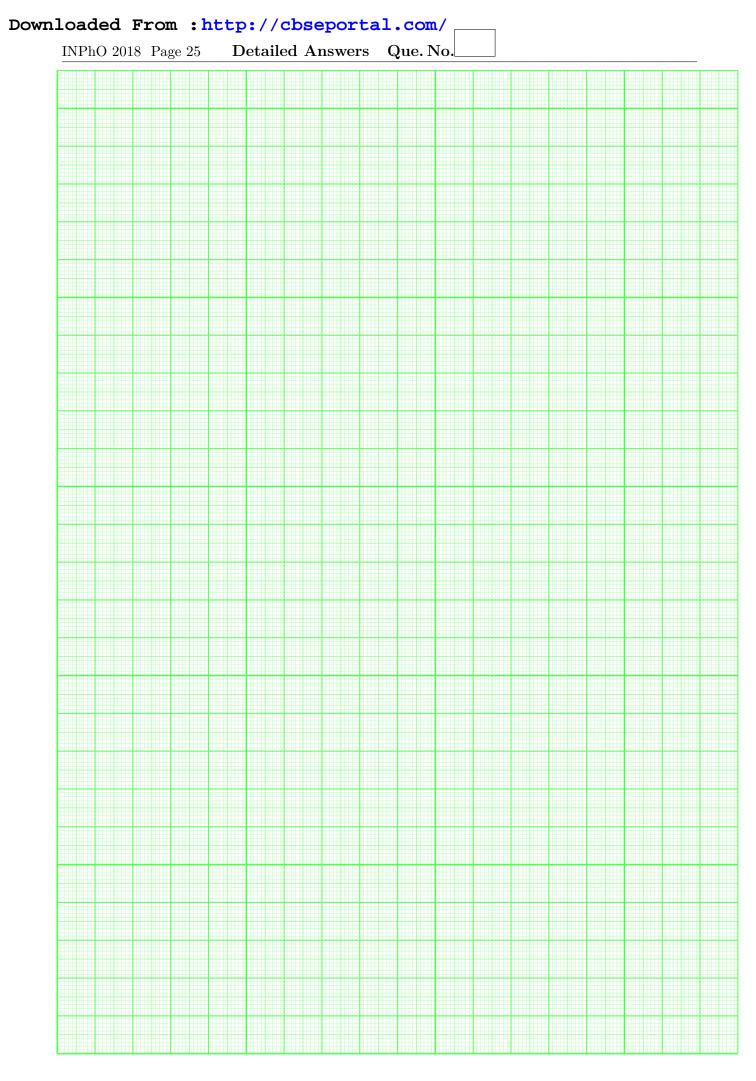
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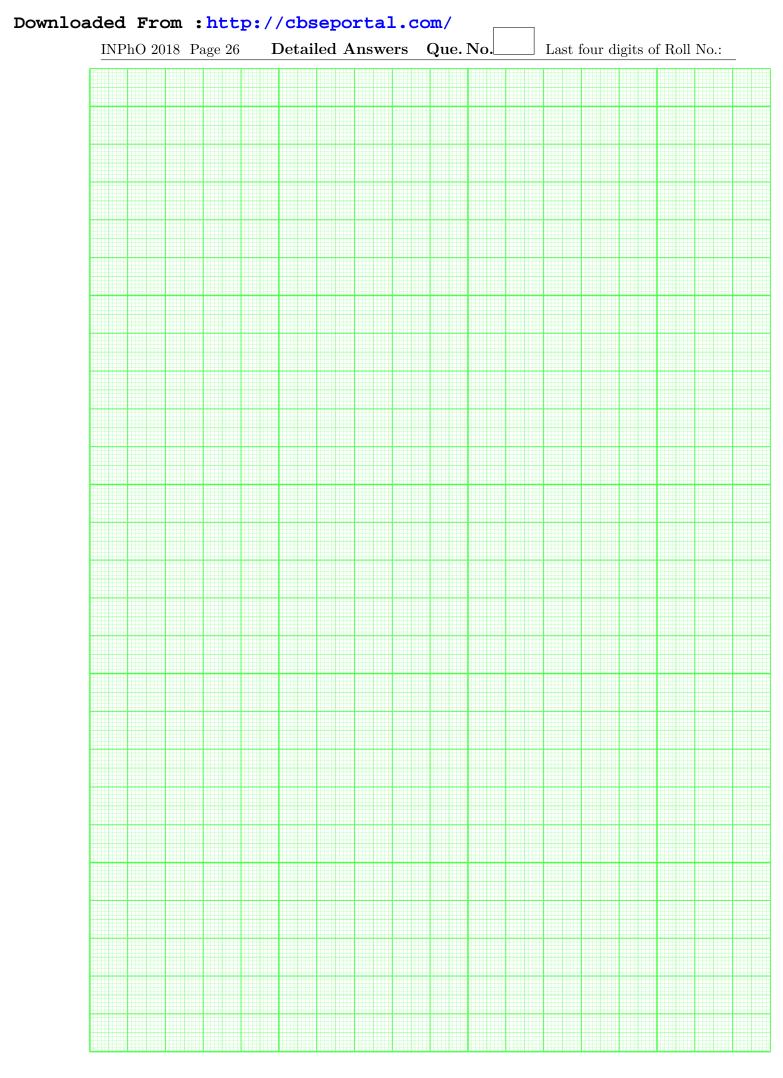
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